

GCE

Further Mathematics B MEI

Y422/01: Statistics major

A Level

Mark Scheme for June 2022

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

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Text Instructions

1. Annotations and abbreviations

Annotation in scoris	Meaning
✓ and ✗	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
E	Explanation mark 1
SC	Special case
^	Omission sign
MR	Misread
BP	Blank page
Highlighting	
Other abbreviations in mark scheme	Meaning
E1	Mark for explaining a result or establishing a given result
dep*	Mark dependent on a previous mark, indicated by *. The * may be omitted if only previous M mark.
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working
AG	Answer given
awrt	Anything which rounds to
BC	By Calculator
DR	This indicates that the instruction In this question you must show detailed reasoning appears in the question.

2. Subject-specific Marking Instructions for AS Level Mathematics B (MEI)

a Annotations must be used during your marking. For a response awarded zero (or full) marks a single appropriate annotation (cross, tick, M0 or \wedge) is sufficient, but not required.

For responses that are not awarded either 0 or full marks, you must make it clear how you have arrived at the mark you have awarded and all responses must have enough annotation for a reviewer to decide if the mark awarded is correct without having to mark it independently.

It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

Award NR (No Response)

- if there is nothing written at all in the answer space and no attempt elsewhere in the script
- OR if there is a comment which does not in any way relate to the question (e.g. 'can't do', 'don't know')
- OR if there is a mark (e.g. a dash, a question mark, a picture) which isn't an attempt at the question.

Note: Award 0 marks only for an attempt that earns no credit (including copying out the question).

If a candidate uses the answer space for one question to answer another, for example using the space for 8(b) to answer 8(a), then give benefit of doubt unless it is ambiguous for which part it is intended.

b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not always be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.

If you are in any doubt whatsoever you should contact your Team Leader.

c The following types of marks are available.

M

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

A method mark may usually be implied by a correct answer unless the question includes the DR statement, the command words “Determine” or “Show that”, or some other indication that the method must be given explicitly.

A

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

B

Mark for a correct result or statement independent of Method marks.

E

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more ‘method’ steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation ‘dep*’ is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only – differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case, please escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.
Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be ‘follow through’. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

f Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.)

We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so.

- When a value is **given** in the paper only accept an answer correct to at least as many significant figures as the given value.
- When a value is **not given** in the paper accept any answer that agrees with the correct value to **2 s.f.** unless a different level of accuracy has been asked for in the question, or the mark scheme specifies an acceptable range.

NB for Specification A the rubric specifies 3 s.f. as standard, so this statement reads "3 s.f."

Follow through should be used so that only one mark in any question is lost for each distinct accuracy error.

Candidates using a value of 9.80, 9.81 or 10 for g should usually be penalised for any final accuracy marks which do not agree to the value found with 9.8 which is given in the rubric.

g Rules for replaced work and multiple attempts:

- If one attempt is clearly indicated as the one to mark, or only one is left uncrossed out, then mark that attempt and ignore the others.
- If more than one attempt is left not crossed out, then mark the last attempt unless it only repeats part of the first attempt or is substantially less complete.
- if a candidate crosses out all of their attempts, the assessor should attempt to mark the crossed out answer(s) as above and award marks appropriately.

h For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A or B mark in the question. Marks designated as cao may be awarded as long as there are no other errors. If a candidate corrects the misread in a later part, do not continue to follow through. E marks are lost unless, by chance, the given results are established by equivalent working. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

i If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers provided that there is nothing in the wording of the question specifying that analytical methods are required such as the bold "In this question you must show detailed reasoning", or the command words "Show" and "Determine. Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.

j If in any case the scheme operates with considerable unfairness consult your Team Leader.

Question		Answer	Marks	AOs	Guidance
1	(a)	P(2 meteors) = 0.2169	B1 [1]	1.1	

Question		Answer	Marks	AOs	Guidance
1	(b)	$P(> 3 \text{ meteors}) = 1 - 0.9662$ $= 0.0338$	M1 A1 [2]	1.1 1.1	Or $[P(> 3 \text{ meteors}) =] 1 - P(\leq 3 \text{ meteors})$ BC
1	(c)	Mean $= 10 \times 1.2 = 12$ $P(\leq 8 \text{ meteors}) = 0.1550$	B1 B1 [2]	3.3 1.1	BC
1	(d)	Meteors occur randomly, independently and at a uniform average rate	E1 E1 [2]	2.2b 2.4	Allow 'constant average rate' and 'same average rate' No context needed due to question giving context Needs to have 'constant' oe and 'average' oe Not 'overall'

2	(a)	Five A $\sim N(5 \times 23, 5 \times 2.8^2)$ $N(115, 39.2)$ $P(\geq 120) = 0.212$ (0.212262...)	B1 M1 A1 [3]	3.3 1.1 3.4	For N and mean For variance BC
2	(b)	Three A – two B $\sim N(3 \times 23 - 2 \times 35, 3 \times 2.8^2 + 2 \times 3.6^2)$ $N(-1, 49.44)$ $P(3 \text{ A last longer}) = 0.443$ (0.443453 ...)	B1 M1 A1 [3]	3.3 1.1 3.4	For N and mean Allow mean = +1 For variance BC
2	(c)	Because adding variances only gives the correct combined variance if the variables are independent.	E1 [1]	2.3	Ignore comments about Expectation

3	(a)	$b + 0.48 + 0.96 + 4b^2 = 1.8$ $b = 0.2$ $a + b + b^2 + 0.24 + 0.32 = 1 \Rightarrow a = 0.2$	M1 A1 B1 [3]	3.1a 1.1 1.1	BC FT $0.44 - b - b^2$
3	(b)	$E(Y) = 10 - 3 \times 1.8 = 4.6$ $\text{Var}(X) = 1.44$ $\text{Var}(Y) = 9 \times 1.44 = 12.96$	B1 B1 B1 [3]	1.1 3.1a 1.1	BC Can get B1 implied by correct answer to $\text{Var}(Y)$ FT their $\text{Var}(X)$

Question		Answer	Marks	AOs	Guidance
4	(a)	$P(X \geq 10) = \frac{k-9}{k}$ or $1 - \frac{9}{k}$	M1 A1 [2]	3.1a 1.1	Allow M1 for numerator $k - 10$ or answer $1 - \frac{10}{k}$
4	(b)	Probability of 1 card being less than 9 = 0.4 $0.4^2 + 2 \times 0.4^2 \times 0.6 + 3 \times 0.4^2 \times 0.6^2$ $= 0.5248$ or $\frac{328}{625}$	B1 M1 A1 [3]	3.1a 1.1 1.1	For 0.4 or 0.6 seen Allow with their 0.4 and 0.6. Allow one coefficient incorrect. OR using $X \sim B(4, 0.6)$ OR using $X \sim B(4, 0.4)$ $P(X \leq 2) = 0.5248$ $1 - P(X \leq 1) = 0.5248$

5	(a)	$P = 0.01145t + 1.786$	M1 A1 [2]	3.3 1.1	For either 0.01145 or 1.786 (1.7858444) BC Allow 3sf
5	(b)	Residual for 28 = $2.114 - (0.01145 \times 28 + 1.786)$ or Residual for 36 = $2.192 - (0.01145 \times 36 + 1.786)$ Residual for 28 = 0.007 Residual for 36 = -0.006	M1 A1 A1 [3]	1.1a 1.1 1.1	Allow if wrong way around Allow 0.006 to 0.008 Allow without referring to part (a) Allow -0.007 to -0.005
5	(c)	The fit is good as the residuals are all fairly small and there is no discernible pattern to suggest that the fit is non-linear	E1 E1 [2]	2.2a 1.1	Must be with reference to residuals Do not allow 'Sum of residuals is small' Allow 'residuals not in blocks'
5	(d)	Temperature 25°C Pressure $\approx 2.07(2)$ Temperature 10°C Pressure $\approx 1.90(0)$	B1 B1 [2]	1.1 1.1	FT awrt 2.07 FT awrt 1.90 If both given to 1dp allow MAX B0B1. If either given to <u>more</u> than 3dp allow MAX B0B1
5	(e)	Because the residuals are small, (and it is interpolation), the first prediction likely to be reliable. The second prediction is rather less reliable because it is extrapolation.	E1 E1 [2]	2.2a 3.5b	Allow 'As points lie close to the line' If only mention interpolation/extrapolation MAX E1E0

Question		Answer	Marks	AOs	Guidance
6	(a)	<p>DR</p> $\text{Est of pop variance} = \frac{6050.3 - \frac{491.84^2}{40}}{39}$ $= \frac{2.63536}{39} = 0.06757$ <p>Confidence interval is 12.296 ± 1.96 $\times \sqrt{\frac{0.06757}{40}}$ or $\times \frac{0.25994}{\sqrt{40}}$ $= 12.296 \pm 0.081$ or (12.215, 12.377) Allow 12.296 ± 0.080 or (12.216, 12.376)</p>	<p>M1</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>[6]</p>	<p>1.1</p> <p>1.1</p> <p>1.1</p> <p>3.3</p> <p>1.1</p> <p>3.4</p>	<p>Accept denominator of 40 rather than 39 for M1</p> <p>Allow 0.676 Or sd = 0.25994</p> <p>or $\frac{491.84}{40}$ seen anywhere</p> <p>Accept <i>t</i>-value of 2.02</p> <p>Accept based on <i>t</i>-distribution (12.213, 12.379) Allow 12.22 to 12.38</p>
6	(b)	It does support the belief because the confidence interval does not contain 12.2	<p>E1</p> <p>[1]</p>	3.5a	Must be unassertive EG do not allow 'the researcher is correct' FT their interval
6	(c)	A random sample enables proper inference about the population to be undertaken	<p>E1</p> <p>[1]</p>	2.4	Do NOT allow 'so that the distribution can be modelled by a Normal...' oe
6	(d)	<p>Sample mean = 1.3</p> $0.098 = 1.96 \times \sqrt{\frac{0.25}{n}}$ <p>Sample size = 100</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>[3]</p>	<p>1.1</p> <p>3.1b</p> <p>1.1</p>	Do not allow M1 for 0.25 rather than $\sqrt{0.25}$

Question		Answer	Marks	AOs	Guidance
7	(a)	$P(X=5) = 0.7^4 \times 0.3$ =0.07203	M1 A1 [2]	3.3 1.1	Allow 0.072
7	(b)	$P(X>3) = 0.7^3 = 0.343$ Use of binomial (6, their 0.343) $P(\text{At least 4 out of 6}) = 1 - 0.8900 = 0.1100$	B1 M1 A1 [3]	1.1 3.3 1.1	With their 0.343 but not 0.3 or 0.7. Must be stated if not 0.343 Allow 0.110
7	(c)	$(1-p)p = \frac{28}{121}$ $\Rightarrow 121p^2 - 121p + 28 = 0$ $p = \frac{4}{11}$ or $p = \frac{7}{11}$	M1 M1 A1 [3]	3.1a 2.1 1.1	Allow sign errors BC Allow 0.363... and 0.636...

Question		Answer	Marks	AOs	Guidance																								
8	(a)	The other student is incorrect since both variables are random so it is equally correct to plot the variables either way around.	E1 E1 [2]	2.2a 2.4	Condone ‘one variable does not affect the other’ or ‘both variables are independent’ Dependent on first mark																								
8	(b)	Because the scatter diagram does not appear to be elliptical due to the outliers so the distribution is probably not bivariate Normal.	E1 E1 [2]	3.5a 2.4	For elliptical For full answer (dependent on first mark) Condone 2 clusters instead of outliers																								
8	(c)	<p>DR</p> <table border="1"> <tr><td>Rank B</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td><td>11</td></tr> <tr><td>Rank F</td><td>1</td><td>6</td><td>2</td><td>8</td><td>5</td><td>7</td><td>9</td><td>4</td><td>3</td><td>10</td><td>11</td></tr> </table> <p>Spearman’s rank coefficient = 0.5909</p> <p>H_0: There is no association between Butterfly and Freestyle times in the population</p> <p>H_1: There is some association between Butterfly and Freestyle times in the population</p> <p>For $n = 11$, 5% critical value is 0.6182</p> <p>$0.5909 < 0.6182$</p> <p>Do not reject H_0. There is insufficient evidence to suggest that there is association between Butterfly and Freestyle times [in the population]</p>	Rank B	1	2	3	4	5	6	7	8	9	10	11	Rank F	1	6	2	8	5	7	9	4	3	10	11	M1 M1 A1 B1 B1 M1 A1 [8]	1.1 1.1 1.1 3.3 1.2 3.4 1.1 2.2b	For ranking Butterfly For ranking Freestyle Allow M1M1 for $\sum d^2 = 90$ may see $1 - \frac{6 \times 90}{11 \times (121 - 1)}$ BC Allow 0.59 For both. Do not allow correlation Need to see population in one or other of the hypotheses for second B1 For comparison provided $ r_s < 1$ (provided sensibly obtained) and sensible critical value eg 0.6021 Do not FT their r_s . Must be in context. Do not allow correlation No marks for PMCC test
Rank B	1	2	3	4	5	6	7	8	9	10	11																		
Rank F	1	6	2	8	5	7	9	4	3	10	11																		
8	(d)	If the test had been done at a different level, the conclusion may have been different Or A 5% significance level means that you will come to the wrong conclusion 5% of the time.	E2 [2]	2.2b 2.4	Oe EG ‘With a different sample the results might be different’ Allow E1 for ‘The conclusion of a hypothesis test is never certain’																								

Question		Answer	Marks	AOs	Guidance
9	(a)	$P(X \leq 7) = \frac{8}{21}$	B1 [1]	1.1	Allow 0.381
9	(b)	$E(X) = 10$ $\text{Var}(X) = \frac{1}{12}(21^2 - 1)$ $= \frac{110}{3}$	B1 M1 A1 [3]	1.1 1.2 1.1	Allow M1 for $\text{Var}(X) = \frac{1}{12}(20^2 - 1)$ Or 36.7 or better
9	(c)	$P(Y \leq 7) = \frac{4}{25}$	B1 [1]	1.1	
9	(d)	Because $\text{Var}(Y) = \frac{\text{Var}(X)}{10}$ and so values of Y are more likely to be closer to the mean than values of X . ($E(X)$ and $E(Y)$ are both 10)	B1 B1 [2]	2.2a 2.4	Allow $\text{Var}(Y) < \text{Var}(X)$ If they get $\text{Var}(Y) = \text{Var}(X) / 100$ or other error then B0 even if then say $\text{Var}(Y) < \text{Var}(X)$ oe
9	(e)	$\text{Var}(W) = \frac{11}{9}$ By CLT distribution is approx $N\left(10, \frac{11}{9}\right)$ $P(W \leq 7)$ with CC is $P\left(Z \leq 7 \frac{1}{60}\right)$ 0.00348	B1 M1 B1 A1 [4]	1.1 2.2a 3.4 1.1	Allow their $\frac{\text{Var}(X)}{30}$ Using their mean from (b) and their $\text{var}(W)$ For CC (Continuity correction) Allow 3 marks for 0.00333 (0.0033278...) (No CC) Allow 0.0035 Allow equivalent method eg using total rather than mean

Question		Answer	Marks	AOs	Guidance
10	(a)	$\text{Low-normal} = \frac{32 \times 12}{60} = 6.4$, $\text{Low-high} = \frac{28 \times 12}{60} = 5.6$ $\text{Medium-normal} = \frac{32 \times 31}{60} = 16.5333$ $\text{Medium-high} = \frac{28 \times 31}{60} = 14.4667$	B1 B1 [2]	3.4 1.1	B1 for any one correct B1 for the other 3 (by subtraction)
10	(b)	$\frac{(5 - 9.0667)^2}{9.0667} = 1.8240$	M1 A1 [2]	1.1 1.1	For $\frac{(O - E)^2}{E}$
10	(c)	DR H_0 : no association between dietary fat intake and cholesterol level H_1 : some association between dietary fat intake and cholesterol level Test statistic = 6.4508 Degrees of freedom = 2 Critical value = 5.991 $6.4508 > 5.991$ so reject H_0 There is sufficient evidence to suggest that there is some association between dietary fat intake and cholesterol level.	B1 B1 B1 B1 M1 A1 [6]	2.5 1.1 3.3 1.1 2.2b 3.5a	For both Allow independent/not independent. Do NOT allow relationship in place of association BC Accept awrt 6.45 Can be implied by correct critical value Allow $\chi^2(6.4508) = 0.9603$ With the above allow comparison with 95% so reject for H_0 M1 Must have correct test statistic and critical value If hypotheses wrong way around allow MAX B0B1B1B1M0A0
10	(d)	For low dietary fat, the contribution of 1.0563 shows that more people than expected have normal cholesterol level whereas the contribution of 1.2071 shows that fewer than expected have high cholesterol level. For medium dietary fat, the numbers are as expected. For high dietary fat, the contribution of 1.8240 shows that fewer people than expected have normal cholesterol level whereas the contribution of 2.0846 shows that more than expected have high cholesterol level	B3,2,1 , [3]	2.2b 3.5a 3.5a	B3 for 5 correct contribution comments B2 for 4 correct contribution comments B1 for two correct comments Allow slightly fewer with higher and slightly more with normal

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